Content

Course Code Course Name Semester Theory Practice Lab Credit ECTS

MAT204 Abstract Algebra 3 3 2 0 5 8

Prerequisites

Admission Requirements

Language of Instruction French
Course Type Compulsory
Course Level Bachelor Degree

Objective To introduce some basic algebraic structures (groups and rings) and how to study them

Groups as symmetry measuring constructs, subgroups, normal subgroups, quotient groups, group homomorphisms,

Content isomorphism theorems, group actions

Rings, subrings and ideals, isomorphism theorems, irreducible and prime elements

Mathématique L3 Algèbre, Aviva Szpirglas

Abstract Algebra: Theory and Applications, Thomas W. Judson, Robert A. Beezer

http://abstract.ups.edu/aata/aata.html

References

An Inquiry Based Approach to Abstract Algebra, Dana C. Ernst

https://danaernst.com/teaching/mat411f20/IBL-AbstractAlgebra.pdf

Cebir I - Temel Grup Teorisi, Ali Nesin

https://nesinkoyleri.org/wp-content/uploads/2019/05/cebir.pdf

Theory Topics

## Weekly Contents

- 1 Notion of symmetry
- 2 Axiomatic definition of a group, group examples, operation tables, subgroup
- 3 Group homomorphisms, operations on groups
- 4 Kernel et image of homomorphisms, quotient of a group by a subgroup, Lagrange's theorem
- Normal subgroups, quotient groups, Isomorphism theorems
- 6 Semi-direct products
- 7 Group actions on sets
- 8 Midterm
- 9 Orbit-stabiliser theorem, Sylow Theorems
- 10 Sylow Theorems and applications
- 11 Rings, ring homomorphisms, kernel and image of homomorphisms, subrings and ideals
- 12 Quotient rings, isomorphism theorem
- 13 Prime and irreducible elements
- 14 Unique Factorization Domains