

Content

| Course Code | Course Name | Semester | Theory | Practice | Lab | Credit | ECTS |
|-------------|-------------------|----------|--------|----------|-----|--------|------|
| MATH 501 | Advanced Analysis | 1 | 3 | 0 | 0 | 3 | 8 |

| | |
|------------------------|--|
| Prerequisites | |
| Admission Requirements | |

| | |
|-------------------------|---|
| Language of Instruction | Turkish |
| Course Type | Compulsory |
| Course Level | Masters Degree |
| Objective | The course aims to cover some parts of the content of Mat 101,102, 201, 202, 301,331 and 452 given in the undergraduate level at Galatasaray University. We try to understand definitions, theorems, and proofs of some results in Real Analysis. We don't prove everything but will try to get a deeper understanding and hope to consolidate your understanding in Real Analysis. |
| Content | <ol style="list-style-type: none"> 1. Analytic functions, harmonic functions. 2. Cauchy-Riemann equation. 3. Cauchy integral theorem 4. Cauchy integral formula 5. Riemann Integral for several variable functions, Fubini's theorem. 6. Lebesgue Outer measure. Measurable sets in \mathbb{R}, then in \mathbb{R}^n 7. Measurable Functions 8. Completion of a Measure space 9. Lebesgue Integral 10. Properties of Lebesgue Integral 11. Comparison of Riemann and Lebesgue Integrals, Convergence Theorems 12. Lebesgue Integral in \mathbb{R}^n, Fubini's theorem for Lebesgue Integral 13. L^p spaces, Convolution 14. Jordan and Hahn Decompositions, Radon-Nikodym Theorem |
| References | <ol style="list-style-type: none"> 1) A. W. Knap, Basic Real Analysis, with an appendix "Elementary Complex Analysis", Digital Second Edition, 2016. 2) G.B. Folland, Real Analysis: Modern Techniques and Their Applications, 1999. 3) W. Rudin, Real and Complex Analysis, McGraw-Hill Inc., 1966. |

Theory Topics

| Week | Weekly Contents |
|------|---|
| 1 | Finite and infinite sets, countability. |
| 2 | Interchange of Limits, Pointwise Convergence, Uniform Convergence |
| 3 | Riemann Integral |
| 4 | Metric Spaces, Open/Closed sets, Compactness, Completeness, Examples: $C(S)$ and $B(S)$ |
| 5 | Riemann Integral for several variable functions, Fubini's theorem. |
| 6 | Lebesgue Outer measure. Measurable sets in \mathbb{R} , then in \mathbb{R}^n |
| 7 | Measurable Functions |
| 8 | Completion of a Measure space |
| 9 | Lebesgue Integral |
| 10 | Properties of Lebesgue Integral / Midterm |

| Week | Weekly Contents |
|------|--|
| 11 | Comparison of Riemann and Lebesgue Integrals, Lebesgue Convergence Theorems |
| 12 | Lebesgue Integral in \mathbb{R}^n , Fubini's theorem for Lebesgue Integral |
| 13 | L^p spaces, Convolution |
| 14 | Jordan and Hahn Decompositions, Radon–Nikodym Theorem |